Corrections and clarifications to

Nonlinear Potential Theory on Metric Spaces,

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- **p. 6, l. -7.** Replace " ε -net" by " 5ε -net".
- **p. 21, l. 13–14.** Replace "Then there exist upper gradients g_j so that" by "Then there is $\tilde{\rho} \in L^p(X)$ such that $g_j := g + \tilde{\rho}/j, \ j = 1, 2, ...,$ are upper gradients. If moreover $g < \infty$ a.e., then".
- **p. 21, l. 20–21.** Replace the last two sentences by "Let finally $\tilde{\rho} = \rho + \infty \chi_{g' \neq g}$ and $g_j = g + \tilde{\rho}/j$. Then g_j is an upper gradient of f. If moreover $g < \infty$ a.e., then (1.6) holds."
- **p. 36.** Add the sentence "Proposition 1.14 is from Cheeger [91]."
- **p. 39, l. 9, 10,** -4. Replace f_{i_k} by f_{l_k} .
- p. 46, l. 20. Delete "minimal".
- **p. 46, l. 21.** Add the sentence "Moreover, $|\varphi' \circ u|g_u$ is a minimal p-weak upper gradient of $\varphi \circ u$, provided that φ is Lipschitz, $\varphi \circ u \in D^p(X)$ or $|\varphi' \circ u|g_u \in L^p(X)$."
- **p. 47, l. 1.** After 2.14 add ", where the last inequality is only required to hold if $\varphi \circ u \in D^p(X)$ ".
- **p. 47, l. 8–9.** Replace these lines by "Lemma 2.14 and (2.5) imply that $|\varphi' \circ u|g_u$ is a p-weak upper gradient of $\varphi \circ u$. Hence $|\varphi' \circ u|g_u \geq g_{\varphi \circ u}$ a.e. if $\varphi \circ u \in D^p(X)$, which in particular holds if $|\varphi' \circ u|g_u \in L^p(X)$, which in turn is true if φ is Lipschitz. To show the minimality in this case, observe that (2.5) and (2.4) yield"
- **p. 47, l. 17–18.** Replace sentence by "Then g_u/u is a p-weak upper gradient of $v = \log u$, which is minimal if $v \in D^p(X)$ or $g_u/u \in L^p(X)$."
- **p. 61, l. 10.** Insert "and p > 1" after "space".
- **p. 62, l. 13, 15.** To avoid confusion between g_1 , g_2 and g_j , replace g_j by \tilde{g}_j .
- p. 64, l. 14–15. Replace sentence by "Lemma 2.37 for open E appeared in [45]." (When [49] was finalized the proof of Lemma 2.37 was omitted, and so the book is the original reference for Lemma 2.37 in the general form.)
- **p. 88 l.** -3. Replace by

$$\infty = \left(f_B |u - u_B|^q d\mu \right)^{1/q} = \lim_{j \to \infty} \left(f_B \min\{j, |u - u_B|^q\} d\mu \right)^{1/q}$$
$$= \lim_{j \to \infty} \lim_{k \to \infty} \left(f_B \min\{j, |u_k - (u_k)_B|^q\} d\mu \right)^{1/q} \le C \operatorname{diam}(B) \left(f_{\lambda B} g^p d\mu \right)^{1/p},$$

Alternatively Fatou's lemma can be used.

- **p. 107, l. -2.** Replace "complete" by "proper".
- **p. 131, l. 5.** Replace $u \ge \frac{1}{2}$ by $u(x) \ge \frac{1}{2}$.
- **p. 145, l. 15.** Replace $||g_u^p||_{L^p(X)}$ by $||g_u||_{L^p(X)}^p$.
- **p. 145, l. -8.** Replace $C(r^p + 1)$ by $C(r^p + 1)\mu(2B)$.
- p. 155, l. 19. Replace "Lemma 1.39" by "Corollary 1.39".
- **p. 159, l. -8.** Insert "Assume that supp μ is locally compact." before "If".
- **p. 169, l. 1.** Replace 6.7 (xi) by 6.19 (x).
- **p. 182, l. -7.** Replace "open" by "bounded open".
- **p. 246, l. −12.** Replace [46] by [45].
- **p. 259, l. 5.** Insert "Let $h_j = \max\{f_j, \psi_j\}$. As $h_j f_j = (\psi_j f_j)_+ \in N_0^{1,p}(\Omega)$, by Proposition 7.4, we have $h_j \in \mathcal{K}_{\psi_j, f_j}$." before "Let".

p. 259, l. 9–10. Replace by

$$||w_j||_{N^{1,p}(X)} \le C||g_{w_j}||_{L^p(\Omega)} \le C(||g_{u_j}||_{L^p(\Omega)} + ||g_{f_j}||_{L^p(\Omega)})$$

$$\le C(||g_{h_j}||_{L^p(\Omega)} + ||g_{f_j}||_{L^p(\Omega)}) \le C(||f_j||_{N^{1,p}(\Omega)} + ||\psi_j||_{N^{1,p}(\Omega)}) \le C$$

p. 259, l. 12. Replace by

$$||u_j||_{N^{1,p}(\Omega)} \le ||w_j||_{N^{1,p}(\Omega)} + ||f_j||_{N^{1,p}(\Omega)} \le C(||f_j||_{N^{1,p}(\Omega)} + ||\psi_j||_{N^{1,p}(\Omega)}) \le C.$$

- $\begin{array}{ll} \textbf{p. 278, l. 18} \ \ \text{Replace "} \sup_{\partial B'} \text{" by } \sup_{\partial B'} u". \\ \textbf{p. 345, l. 6} \ \ \text{Replace "} 1$
- **p. 348, l. 9** Insert " $l_{\gamma} \leq Ad(x, y)$ and" after "such that".
- p. 371, [44] Add "on metric spaces" after "obstacle problem".
- p. 371, [45] Add "on metric spaces" after "obstacle problem".
- p. 372, [56] Add "in metric spaces" after "functions".